

# Functional Style

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But we have to have repetition to have useful programs

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## Recursion

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One is that it leads naturally to having functions as *first class objects*

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- passed into a function as an argument
- returned from a function as a result

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Again, a trivial (and contrived) example of a much bigger idea

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Exercise. Investigate

```
double foo(double x) {  
    return (x > 0.0 ? sin : cos)(3.0);  
}
```

in C

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List: do the current value; recurse on the rest of the list

Tree: do the current value; recurse on the left subtree; recurse on the right subtree

We will find that the idea of separating the action of traversal of a datastructure from the operation on the elements of the datastructure is prominent in the functional style

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Some were designed from scratch as functional



# Functional Style

Just a few names

- Lisp/Scheme (1959)
- APL (1964) “A Programming Language”
- ISWIM (1966) “If you See What I Mean”
- SASL (1972) “St. Andrews Static Language”
- ML/SML (1973) “Meta Language”
- Hope (1980)
- KRC (1981) “Kent Recursive Calculator”
- Miranda (1985)
- Erlang (1987)
- Haskell (1990)
- OCaml (1996)

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Java has just introduced first class functions (lambdas)

Though there have been many previous attempts to add functional style to Java, e.g., Pizza

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Later we shall look at *metabobject protocols* where the behaviour of a OO system can be altered within the program

If you don't like the way methods are chosen, or the way slots are accessed in an object, change it

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Two languages that look and feel very different, but both embrace the functional idea

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- Really a *family* of languages

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- Standardised as “Haskell 98”

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- Haskell is *non-strict* and *lazy*

Strict and eager is what you are used to from other languages

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So Lisp will look strange but act as you might expect

And Haskell will look relatively normal but act quite weirdly

# Lisp

We start with Lisp

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*“Lisp is worth learning for the profound enlightenment experience you will have when you finally get it; that experience will make you a better programmer for the rest of your days, even if you never actually use Lisp itself a lot.”*

Eric Raymond, “How to Become a Hacker”

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By the time we get to Haskell we should be able to say “and such-and-such is just like Lisp” and just concentrate on their differences

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Not designed for numerical processing (Fortran did that), but manipulation of symbols

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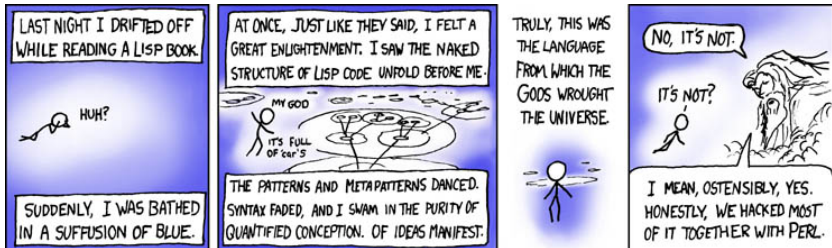
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We could do an entire unit on it

# Lisp History



<http://xkcd.com/224/>

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Symbols look like variables in other languages, but are objects in their own right

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That is, pushing symbols about, just like in mathematics

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It is the only object that is both a list and an atom



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each of which is a list itself

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Thus Lisp can easily be used to represent non-numeric data

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With a Lisp program you can't tell

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All functions are like this, even things like  $+$  that are treated specially by other languages

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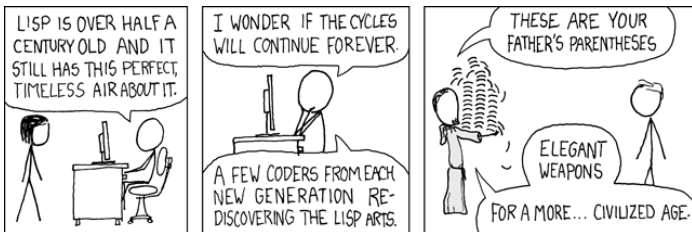
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And has exactly the right number of parentheses!

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<http://xkcd.com/297/>

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(+ (pow (sin x) 2) (pow (cos x) 2))
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for  $\sin^2 x + \cos^2 x$

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The *reason* for this syntax is very important