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A trade-off of compiler speed against coding speed



Python allows optional type declarations for variables:

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 return n+n



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def double(n: int):
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Though this is purely documentary and not checked by the runtime: double(3.14) -> 6.28 and double('ha') -> 'haha'



Such documentary type declarations (also called *type hints*)

- make the code easier to understand for the programmers
- makes the code easier to refactor
- helps IDEs (e.g., autocompletion)
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Exercise There are several static type checkers for Python (Mypy, Pytype, Pyright, Pyre, ...). Why do these exist?



Exercise Read about Hindley-Milner type systems

Exercise Elements of type inference is being adopted by some traditional explicitly typed languages. Why? Read about auto in C++, var in C# and var in Java

Exercise Think about type inference in the presence of automatic type coercions (weak typing)



Static types are often further divided:

 Monomorphic/Lexical: variables have a single, definite type, so you can type-check purely on the variables int f(int x) { ... y = x; ... }

A very common approach



 Polymorphic: types can be shown by type variables, e.g., push: a * [a] -> [a] or template <class T> List<T> push(T x, List<T> 1)



Or

public static <T> List<T> push(T x, List<T> 1)
or

```
func push[T](x T, 1 []T) []T
```

where a and T are variables that stand for types, not values

So push is a function that takes a value of some type, a list of values of the same type and returns a list of values of that type





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That is, you could give it an argument of type A or an argument of type B and the function would (a) work and (b) do the "same thing" to the argument regardless of the actual type of the argument, e.g., push, above



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The function ${\tt push}$ works the same on lists of integers and lists of strings



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After all, this is one of the reasons types are used: to catch the cases where you use a value of the wrong type



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But the word "polymorphic" has expanded to mean something more complicated



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Multiple different functions with the same name

The compiler can distinguish which f we mean by the argument types: f(2) means the int function; while f(2.0) means the double function



And for f(x) the compiler looks at the declared type for x to see which f to use



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And different chunks of code are compiled for each function



Aside: another reason why we need to be careful to distinguish between, say, 2 and 2.0



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Exercise Think about the call f(3/2)



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Overloading does not *prevent* you making the various fs do wildly different things: but doing this would only make understanding your code harder



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In fact, in a typical implementation, the compiler internally renames ("name mangling") the two functions as (something like) f_int and f_double, so giving them distinct names


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It then compiles this "rewritten" code



Overloading is very widespread and appears in a limited way in lots of languages: common functions like + are often overloaded

Remember that operators like + and * are just convenient syntax for the expected underlying functions or methods and otherwise are not particularly special

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Many languages overload operators, so, for example, allowing int+int and double+double values, sometimes strings, too

Some languages allow mixed types, too: int+double and double+int, as in 1 + 2.3

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These can all refer to different underlying functions. E.g., int+double would likely coerce its first argument to a double before doing a double+double add. This is different from what double+int needs to do

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Exercise Some languages (e.g., C++, Rust, Python) allow you to define your own methods on operators, while others don't (e.g., Java). Investigate





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length [2] (list of integers) runs the same code as length ["hello" "world"] (list of strings)

length doesn't care about the types of its arguments



Beware of overloading disguised as polymorphism:

```
template <class T> // T is a type variable
T f(T x) { return -x; }
```

in C++ defining a function f taking a value of type T and returning a value of type T, for all types T. Similarly:

```
// T any type that implements negation ff f<T>(x: T) -> T where T: Neg<Output=T> { -x }
```

in Rust.

Both allow us to call f(2) and f(2.0) etc.



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Exercise Make sure you understand why negation of integers is different code to negation of floating point



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For them, the fact that two functions have the same name is enough to call it polymorphism

Perhaps they are thinking of overloading the *name*, rather than overloading the *function*?

They call it *ad hoc polymorphism*, in contrast with true polymorphism, *parametric polymorphism*

overloading	\leftrightarrow	ad hoc polymorphism
polymorphism	\leftrightarrow	parametric polymorphism



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int f(int n) { ... }
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This is much rarer

Types Overloading Return Types

For example

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int f(int n) { ... }
double f(int n) { ... }
int g(int n) { ... }
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What should we do with g(f(1))?
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Overloading *both* argument types and return types is tricky: so we pick just one, and overloading arguments is generally more useful



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You *can* have both int foo(int) and double foo(double) by virtue of the different argument types

Exercise Language with more sophisticated type systems, such as Rust and Haskell, do allow a form of overloading on return types. Read about this



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Exercise See *generics* in Java: this uses *Type Erasure* (which is actually parametric polymorphism)

Exercise See *generics* in Go: this uses a partial monomorphization technique called *GCShape stenciling with Dictionaries*



Exercise Swift is superficially similar to other languages, e.g.,

```
func min<T: Comparable>(x: T, y: T) -> T {
  return y < x ? y : x
}</pre>
```

but again, it does something different. Read about *Generic Specialization* (which is kind of dynamic)

Exercise And read about C#'s approach to monomorphization: *Lazy Monomorphisation*



Advanced Exercise Compare these monomorphization techniques

Exercise Find out what overloading your favourite languages support, e.g., overloading based on numbers of arguments to a function: int f(int a) and int f(int a, int b)



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Some languages do support *subtypes*, as opposed to *subclasses*, e.g., positive integers as a subtype of all integers, but this is not common





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But subtype polymorphism — something every OO programmer relies on every day — is not actually different from the kinds of polymorphism we have seen already

Types Subtype Polymorphism

Suppose we have classes

```
class Animal {
  bool alive() { ... }
  bool sleepy() { return false; }
}
class Cat extends Animal {
  bool sleepy() { return true; }
}
```

where ${\tt Cat}$ inherits the <code>alive</code> method but overrides the <code>sleepy</code> method



The alive method is parametric polymorphic: the same method works on more than one type, namely Animal and Cat



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Thus "subtype polymorphic" is actually just a shorthand for "either ad-hoc or parametric polymorphic"





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Suppose S is a subtype of T. Then whenever we need an instance of type T we can use an instance of type S, and our code should still operate correctly



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Methods for Animal should work on Cats



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Some examples later, when we talk about class composition



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Lisp has always had parametric polymorphism (length of a list, etc.)



Hacker Exercise C "supports" polymorphism using void *. Read about this

Exercise Ada supports subtyping, e.g., *integer ranges*, such as "integers 0...10" as a subtype of all integers. Read about this

Exercise We can also have polymorphic *datatypes*, e.g., list in Lisp, struct Pair<T>(T, T) in Rust, Java, and so on. Read about these, and determine whether they are parametric or ad-hoc