

## High Piezoelectric Sensitivity Composites Based on Ferroelectric Ceramics

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This paper describes the modelling and comparison of 0-3 and 3-3 piezocomposites, including three-component structures such as 0-0-3 systems. The piezoelectric properties are calculated for PbTiO<sub>3</sub> based piezocomposites where the anisotropy factor ( $-d_{33}/d_{31}$ ) of the piezoelectric can be varied from small to infinitely large values. Maxima of these parameters are determined and factors influencing piezoelectric sensitivity are analysed.

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Significant improvements in the materials for electromechanical transducers are attained using the composite route and utilising existing piezoelectric materials combined with another phase, such as a polymer or air. Piezoelectric sensitivity is characterised by parameters [1–3], such as the piezoelectric voltage coefficients ( $g_{33}$  and  $g_{31}$ ), piezoelectric figure of merit ( $d_{33} \cdot g_{33}$ ) and hydrostatic figure of merit (HFOM)  $d_h \cdot g_h$ , where the hydrostatic piezoelectric charge coefficient  $d_h = d_{33} + 2d_{31}$ , the hydrostatic piezoelectric voltage coefficient  $g_h = d_h/\epsilon_{33}^T$  and  $\epsilon_{33}^T$  is permittivity along the poling axis ( $OX_3$ ) at constant stress.

A two-figure number describes the piezocomposite [1], which designates the connectivity of the active and inactive phases. ‘0-3’ represents individual piezoelectric particles distributed in a continuous polymer and ‘3-3’ represents interconnected piezoelectric and polymer phases. The aim of this paper is to compare sensitivity parameters of 0-3 and 3-3 PbTiO<sub>3</sub>-based

composites. The advantage of using  $\text{PbTiO}_3$  is that, in addition to varying the connectivity, the anisotropy factor ( $-d_{33}/d_{31}$ ) can be varied [4] from small values, where  $d_{31}$  is large compared to  $d_{33}$ , to infinitely large values, where  $d_{31}$  is small compared to  $d_{33}$ . This has not been examined, which is surprising since the principal benefit of using piezocomposites is to develop a structure with a reduced  $d_{31}$ , higher  $-d_{33}/d_{31}$  and higher  $d_h$  compared to the monolith.

The 0-3 composite is represented by a cubic *Banno unit cell* [5] containing a piezoceramic inclusion surrounded by a matrix. The inclusion is a rectangular parallelepiped and its length, width and height make up the  $t$ th,  $n$ th and  $h$ th parts of the unit-cell edge. The composite is poled along the  $\text{OX}_3$  axis of a rectangular ( $\text{X}_1\text{X}_2\text{X}_3$ ) system. Calculations are carried out using room-temperature elastic, piezoelectric and dielectric constants of  $\text{PbTiO}_3$ ,  $(\text{Pb}_{0.76}\text{Ca}_{0.24})\text{TiO}_3$  and  $\text{Pb}(\text{Zr}_{1-x}\text{Ti}_x)\text{O}_3$  ceramics. The constants were taken from experimental data [6, 7] or evaluated in accordance with an algorithm [4]. The elastic and dielectric constants of the elastomer matrix were from Ref. [2]. The electromechanical constants of the piezoceramic and polymer components are averaged by a matrix method that has been applied to other systems [8]. The averaging procedure determines of the effective constants of a laminated piezoceramic-polymer structure by taking into account the electrical and mechanical boundary conditions at (i)  $x_1 = \text{constant}$ , (ii)  $x_2 = \text{constant}$  and (iii)  $x_3 = \text{constant}$  separately.

The first calculations considers the variation of the composite concentration parameters  $0 < (t, n, h) < 1$ . By variation of  $n$  and  $t$ , maxima of  $g_h$ ,  $d_{33} \cdot g_{33}$  and  $d_h \cdot g_h$  are established. The values of these maxima increase with increasing  $h_0$  (ceramic particle height) and when  $h = 1$  the composite has 1-3 connectivity, where absolute maxima are achieved. Concentration dependences with  $h = 0.95$  and variable  $(t, n)$  are in Fig. 1. These composites display high  $g_h \approx 4 g_h^m$  (Fig. 1a) and  $d_{33} \cdot g_{33} \approx 15 d_{33}^m \cdot g_{33}^m$  (Fig. 1b). The 'm' superscript relates to the monolithic piezoceramic. The location of the  $g_h$  and  $d_{33} \cdot g_{33}$  maxima are at  $t \ll 1$ ,  $n \rightarrow 1$  or  $n \ll 1$ ,  $t \rightarrow 1$ , which correspond to 'plate-like' piezoceramic inclusions along the  $\text{OX}_1$  or  $\text{OX}_2$  axes. The HFOM ( $d_h \cdot g_h$ ) shows a monotonous concentration dependence on both  $t$  and  $n$  as they vary from 0.01 to 0.99 (Fig. 1c). The composite HFOM remains two orders of magnitude lower than bulk  $\text{PbTiO}_3$  due to a discontinuous distribution of the piezoceramic along the poling axis.

The second calculations incorporates disk-like porosity into the polymer matrix. Air inclusions are described by an equation  $(x_1^2/a_1^2) + (x_2^2/a_1^2) + (x_3^2/a_3^2) = 1$  where  $\alpha_{sa} = a_3/a_1$  is the ratio of semiaxes. The porous polymer structure achieves large increases in sensitivity for the 0-0-3 connectivity

composite. Even at low polymer porosity  $m_p = 0.10$  and ratio  $\alpha_{sa} = 0.1$ ,  $g_h$  and  $d_h \cdot g_h$  are 3-4 times larger than those measured on similar 0-3 composites [9] and data in Fig. 1a, c. The improved figures of merit are due to the increased compliances  $s_{11}^p$  and  $s_{12}^p$  and reduced permittivity  $\epsilon_{33}^p$  of the porous polymer.

Increasing piezoelectric sensitivity is associated with increasing the connectivity of the piezoelectric component. In a 3-3 composite the connectivity is increased to three dimensions to create interpenetrating piezoceramic and polymer. The effective parameters  $\epsilon_{33}^T$ ,  $d_h$  and  $g_h$  are calculated as a function of ceramic volume fraction and materials properties using model concepts [10]. The most important results (Fig. 2) show  $d_h$ ,  $g_h$  and  $d_h \cdot g_h$  as a function of ceramic volume fraction for  $\text{PbTiO}_3$ -based composites, where the

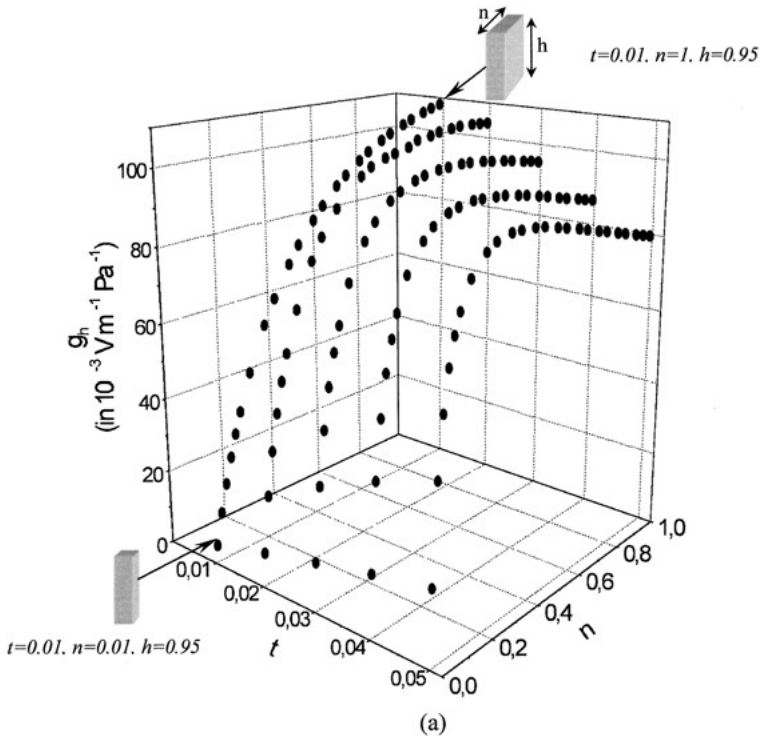
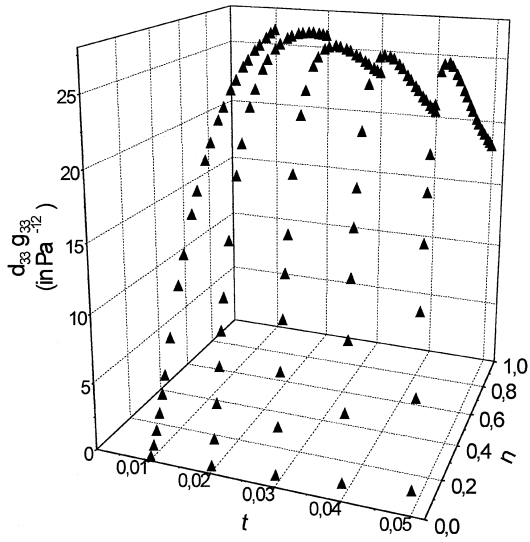
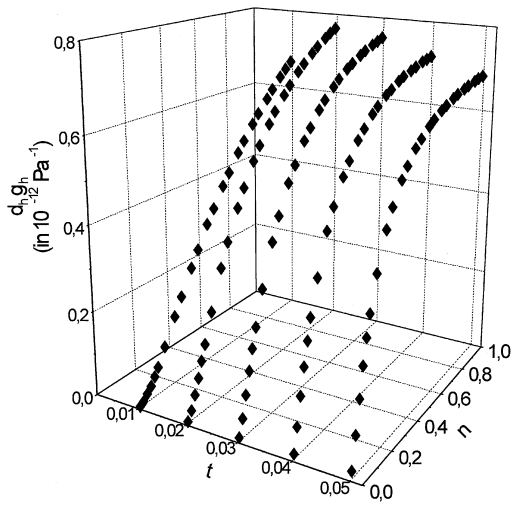


FIGURE 1 Parameters  $g_h$  (a),  $d_{33} \cdot g_{33}$  (b) and  $d_h \cdot g_h$  (c) that characterise piezoelectric sensitivity of the 0-3 composite “modified  $\text{PbTiO}_3$  piezoceramic-elastomer” with inclusions in the form of a rectangular parallelepiped.  $h$ , the particle height along poling direction ( $\text{OX}_3$ ), is 0.95. (Continued)



(b)



(c)

FIGURE 1 (Continued)

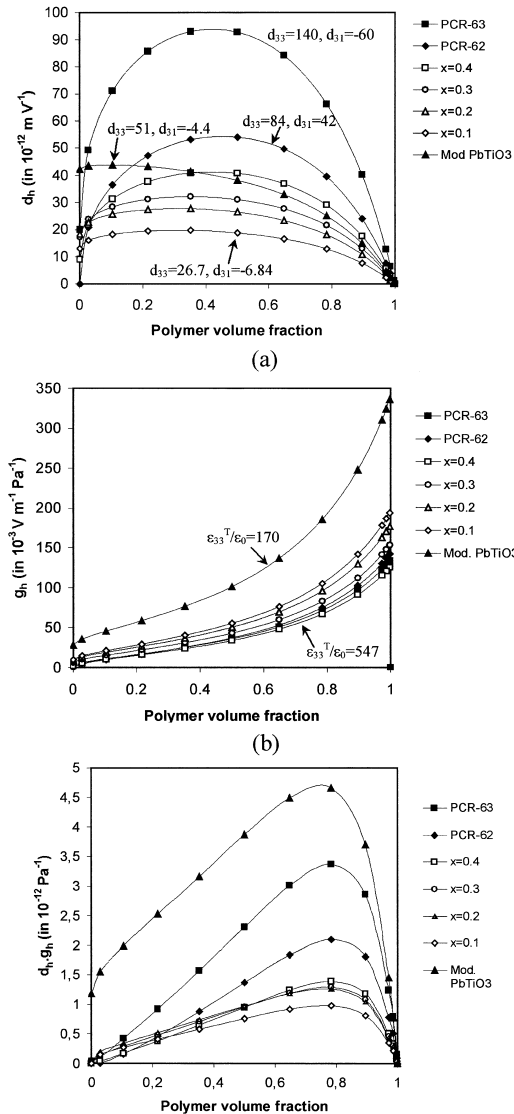


FIGURE 2 Parameters  $d_h$  (a),  $g_h$  (b) and  $d_h \cdot g_h$  (c) calculated for the 3-3 composite “PbTiO<sub>3</sub>-based piezoceramic-polymer.” Ceramics presented include modified PbTiO<sub>3</sub>, PCR-62, PCR-63 and Pb(Zr<sub>1-x</sub>Ti<sub>x</sub>)O<sub>3</sub> where  $x = 0.1, 0.2, 0.3$  and  $0.4$  and the abbreviation “PCR” means “piezoelectric ceramic from Rostov-on-Don” (Pb(Zr<sub>1-x</sub>Ti<sub>x</sub>)O<sub>3</sub> type). Selected  $d_{33}$  and  $d_{31}$  values indicated in  $\text{pC N}^{-1}$ .

polymer component is ten times more compliant than the ceramic. For example,  $d_h$  reaches a maximum at polymer volume fractions  $\sim 0.4$ – $0.5$  for PCR-63, PCR-62 and different solid solutions of  $\text{Pb}(\text{Zr}_{1-x}\text{Ti}_x)\text{O}_3$  (Fig. 2a). The highest composite  $d_h$  values are achieved using piezoceramics with high  $d_{33}$  (PCR-62 and PCR-63). The mechanism by which  $d_h$  increases is similar to that for 1-3's [11]; whereby the structure leads to a large reduction in  $d_{31}$  relative to  $d_{33}$ . Therefore, the ceramics which experience the greatest  $d_h$  enhancement are those with a small anisotropy factor  $-d_{33}/d_{31}$  (i.e. a high  $-d_{31}$ ), such as PCR-62 and PCR-63 (Fig. 2a). Incorporating polymer into modified  $\text{PbTiO}_3$  merely decreases the  $d_{33}$  and  $d_h$  value (Fig. 2a).

The  $g_h$  parameter increases for all the 3-3 composites examined as polymer is introduced into the structure (Fig. 2b); due to the increased  $d_h$  and decreased permittivity. The highest  $g_h$  is for the modified  $\text{PbTiO}_3$ -based composite, mainly due to the low permittivity ( $\epsilon_{33}^{m,T}/\epsilon_0 = 170$ ) [6]. The HFOM ( $d_h \cdot g_h$ ) reaches a maximum at ceramic fractions of  $\sim 0.2$  and, unlike 0-3 composites, large increases are observed compared to the bulk material (Fig. 2c).

## CONCLUSIONS

Our study of 0-3, 0-0-3 and 3-3 piezocomposites based on  $\text{PbTiO}_3$  enables the prediction of concentration dependences of the effective parameters and establish important extreme points of these parameters. Due to the lack of connectivity in 0-3's, piezoelectric strain constants such as  $d_{33}$  and  $d_h$  are low, but the reduced permittivity provides enhanced piezoelectric voltage constants such as  $g_{33}$  and  $g_h$ . High piezoelectric sensitivity depends on ceramic particle microgeometry, ceramic volume fraction and the presence of elongated porosity in the polymer, an area that has not been studied in detail.

The 3-3 materials are more sensitive to the anisotropy factor  $-d_{33}/d_{31}$ . The greatest benefits in  $d_h$  are at high ceramic volume fractions using materials with high  $d_{33}$  and small  $-d_{33}/d_{31}$  ratios, although in all cases the reduced permittivity leads to increased  $g_h$ . The models enable 0-3 and 3-3 composites to be optimised depending on the application and the relevant figure of merit.

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